Large Eddy Simulations of Trade-Wind Cumuli using Particle-Based Microphysics with Monte-Carlo Coalescence

Sylwester Arabas

Institute of Geophysics, Faculty of Physics, University of Warsaw, Poland

Shin-ichiro Shima

Graduate School of Simulation Studies, University of Hyogo, Kobe, Japan

NCAR MMM Seminar Boulder, CO, USA, November 15th 2012



(□▶ ▲圖▶ ▲콜▶ ▲콜▶ ― 道 ─ ののの

Trade-wind cumuli



MODIS image by Robert Wood: http://www.atmos.washington.edu/~robwood/



▲□▶▲圖▶▲콜▶▲콜▶ = 亘 - のへぐ

Trade-wind cumuli: why to study them?

- important for the Earth climate due to contrasting effects on solar and thermal radiation:
 - shortwave: significant change of albedo if clouds present
 - Iongwave: small impact on outgoing thermal radiation (low level)
- > often treated in models as non-precipitating clouds while...



Figure 1. from Rauber et al. 2007 (MWR)

- definition of a shallow-convection model benchmark case inspired by the RICO field campaign (Rauber et al. 2007, MWR)
- comparison of results from 13 different LES models
- selected conclusions:
 - plausibly reproduces many features of the observed layer"
 - "simulations do show considerable departures from one another in the representation of the cloud microphysical structure"
 - "simulations differ substantially in the amount of rain they produce"
 - "these differences appear to be related to microphysical assumptions made in the models"



van Zanten et al. 2011, JAMES:

- definition of a shallow-convection model benchmark case inspired by the RICO field campaign (Rauber et al. 2007, MWR)
- comparison of results from 13 different LES models
- selected conclusions:
 - "simulations agree on the broad structure of the cloud field ... plausibly reproduces many features of the observed layer"

"simulations do show considerable departures from one another in the representation of the cloud microphysical structure"

- "simulations differ substantially in the amount of rain they produce"
- "these differences appear to be related to microphysical assumptions made in the models"



- definition of a shallow-convection model benchmark case inspired by the RICO field campaign (Rauber et al. 2007, MWR)
- comparison of results from 13 different LES models
- selected conclusions:
 - "simulations agree on the broad structure of the cloud field ... plausibly reproduces many features of the observed layer"
 - "simulations do show considerable departures from one another in the representation of the cloud microphysical structure"
 - "simulations differ substantially in the amount of rain they produce"
 - "these differences appear to be related to microphysical assumptions made in the models'



- definition of a shallow-convection model benchmark case inspired by the RICO field campaign (Rauber et al. 2007, MWR)
- comparison of results from 13 different LES models
- selected conclusions:
 - "simulations agree on the broad structure of the cloud field ... plausibly reproduces many features of the observed layer"
 - "simulations do show considerable departures from one another in the representation of the cloud microphysical structure"
 - "simulations differ substantially in the amount of rain they produce"
 - "these differences appear to be related to microphysical assumptions made in the models"



- definition of a shallow-convection model benchmark case inspired by the RICO field campaign (Rauber et al. 2007, MWR)
- comparison of results from 13 different LES models
- selected conclusions:
 - "simulations agree on the broad structure of the cloud field ... plausibly reproduces many features of the observed layer"
 - "simulations do show considerable departures from one another in the representation of the cloud microphysical structure"
 - "simulations differ substantially in the amount of rain they produce"
 - "these differences appear to be related to microphysical assumptions made in the models"





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models υπικ
- ▶ coupled with Lagrangian-in-space ~→ particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models υπικ
- ▶ coupled with Lagrangian-in-space → particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models UNING
- ▶ coupled with Lagrangian-in-space → particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models UNING
- ▶ coupled with Lagrangian-in-space ~→ particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models UNING
- ▶ coupled with Lagrangian-in-space → particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models υπικ
- ▶ coupled with Lagrangian-in-space → particle tracking





- diffusive error-free particle growth schemes
 (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models υνικ
- coupled with Lagrangian-in-space ~> particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models UNER
- coupled with Lagrangian-in-space ~> particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- fewer parameterisation in comparison with bulk or bin models on the parameterisation in comparison with bulk or bin models on the parameterisation in comparison with bulk or bin models.
- coupled with Lagrangian-in-space ~> particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- Fewer parameterisation in comparison with bulk or bin models UNL
- coupled with Lagrangian-in-space ~> particle tracking





- diffusive error-free particle growth schemes (condensational "moving sectional", collisional: Monte-Carlo)
- scales better than ND-bin with number of particle attributes
- Fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparison with bulk or bin models on the fewer parameterisation in comparameterisation in comparison with bulk or b
- coupled with Lagrangian-in-space ~ particle tracking



- ▶ each particle (aka super-droplet) → many "similar" real-world particles
- attributes: multiplicity, dry radius, wet radius, nucleus type, ...
- aerosol, cloud, precip, particles not distinguished, subject to same processes

Eulerian / PDE	
advection of heat advection of moisture	particle transport by the flow condensational growth collisional growth sedimentation
$\partial_t(\rho_d r) + \nabla(\vec{v}\rho_d r) = \rho_d$	$i = \sum_{\text{particles } \in \Delta V} \dots$
$\partial_t(\rho_d\theta) + \nabla(\vec{v}\rho_d\theta) = \rho_d\dot{\theta}$	$\dot{\theta} = \sum_{\text{particles } \in \Delta V} \dots$

- recent examples in context of precipitating clouds:
 - Shima et al. 2009, QJ
 - Andrejczuk et al. 2010, JGR
 - Riechelmann et al. 2012, NJP



- ▷ each particle (aka super-droplet) ~→ many "similar" real-world particles
- attributes: multiplicity, dry radius, wet radius, nucleus type, ...
- aerosol, cloud, precip, particles not distinguished, subject to same processes



- recent examples in context of precipitating clouds:
 - Shima et al. 2009, QJ
 - Andrejczuk et al. 2010, JGR
 - Riechelmann et al. 2012, NJP



- ▷ each particle (aka super-droplet) ~→ many "similar" real-world particles
- attributes: multiplicity, dry radius, wet radius, nucleus type, ...
- ▷ aerosol, cloud, precip. particles not distinguished, subject to same processes



- recent examples in context of precipitating clouds:
 - Shima et al. 2009, QJ
 - Andrejczuk et al. 2010, JGR
 - Riechelmann et al. 2012, NJP



- ▷ each particle (aka super-droplet) ~→ many "similar" real-world particles
- attributes: multiplicity, dry radius, wet radius, nucleus type, ...
- > aerosol, cloud, precip. particles not distinguished, subject to same processes

Eulerian / PDE	Lagrangian / ODE
advection of heat	particle transport by the flow
advection of moisture	condensational growth
	collisional growth
	sedimentation
$\partial_t(ho_d r) + abla(ec{v} ho_d r) = ho_d \dot{r}$	$\dot{r} = \sum \dots$
	particles $\in \Delta V$
$\partial_t(\rho_d\theta) + \nabla(\vec{v}\rho_d\theta) = \rho_d\theta$	$\theta = \sum \dots$
	particles $\in \Delta V$
	the second se

- recent examples in context of precipitating clouds:
 - Shima et al. 2009, QJ
 - Andrejczuk et al. 2010, JGR
 - Riechelmann et al. 2012, NJP



- ▷ each particle (aka super-droplet) ~→ many "similar" real-world particles
- attributes: multiplicity, dry radius, wet radius, nucleus type, ...
- > aerosol, cloud, precip. particles not distinguished, subject to same processes

Eulerian / PDE	Lagrangian / ODE
advection of heat	particle transport by the flow
advection of moisture	condensational growth
	collisional growth
	sedimentation
$\partial_t(ho_d r) + abla(ec{v} ho_d r) = ho_d$	$i = \sum_{\text{particles} \in \Delta V} \dots$
$\partial_t(ho_d heta) + abla(ec v ho_d heta) = ho_d\dot{ heta}$	$\dot{\theta} = \sum_{\text{particles } \in \Delta V} \dots$

- recent examples in context of precipitating clouds:
 - Shima et al. 2009, QJ
 - Andrejczuk et al. 2010, JGR
 - Riechelmann et al. 2012, NJP



- ▷ each particle (aka super-droplet) ~→ many "similar" real-world particles
- attributes: multiplicity, dry radius, wet radius, nucleus type, ...
- > aerosol, cloud, precip. particles not distinguished, subject to same processes

Eulerian / PDE	Lagrangian / ODE
advection of heat	particle transport by the flow
advection of moisture	condensational growth
	collisional growth
	sedimentation
$\partial_t(\rho_d r) + \nabla(\vec{v}\rho_d r) = \rho_d$	$t = \sum \dots$
	$particles \in \Delta V$
$\partial_t(ho_d heta) + abla(ec{v} ho_d heta) = ho_d heta$	$\dot{\theta} = \sum \dots$
	$particles \in \Delta V$
> vecent evenue in context of even	initating alouday

- recent examples in context of precipitating clouds:
 - Shima et al. 2009, QJ
 - Andrejczuk et al. 2010, JGR
 - Riechelmann et al. 2012, NJP



- ▷ each particle (aka super-droplet) ~→ many "similar" real-world particles
- attributes: multiplicity, dry radius, wet radius, nucleus type, ...
- ▷ aerosol, cloud, precip. particles not distinguished, subject to same processes

Eulerian / PDE	Lagrangian / ODE
advection of heat	particle transport by the flow
advection of moisture	condensational growth
	collisional growth
	sedimentation
$\partial_t(\rho_d r) + \nabla(\vec{v}\rho_d r) = \rho_d$ $\partial_t(\rho_d \theta) + \nabla(\vec{v}\rho_d \theta) = \rho_d \dot{\theta}$	$\dot{\theta} = \sum_{\substack{\text{particles} \in \Delta V \\ \dot{\theta} = \sum_{\substack{\sum \dots \\ \text{particles} \in \Delta V}} \dots$

- recent examples in context of precipitating clouds:
 - Shima et al. 2009, QJ
 - Andrejczuk et al. 2010, JGR
 - Riechelmann et al. 2012, NJP

► for all *n* super-droplets in a grid box of volume ΔV in timestep Δt ► each representing a real particles (across) (cloud) drivele (can)

$$P_{ij} = max(\xi_i, \xi_j) \cdot \underbrace{E(r_i, r_j) \cdot \pi(r_i + r_j)^2 \cdot |v_i - v_j|}_{\text{coalescence kernel}} \cdot \frac{\Delta t}{\Delta V} \cdot \frac{n \cdot (n-1)}{2} / \left[\frac{n}{2}\right]$$

- where r drop radii, $E(r_i, r_j)$ collection efficiency, v drop velocities
- ▷ coalescence takes place once in a number of timesteps (def. by P_{ij}) all min (ξ_i, ξ_j) droplets coalesce \rightarrow there's always a "bin" of the right size to store the collided particle
- \blacktriangleright collisions triggered by comparing a uniform random number with P_{ij}
- \blacktriangleright extensive parameters summed (\rightsquigarrow conserved), intensive averaged
- ▶ [n/2] random non-overlapping (i,j) pairs examined only cost: $O(n^2) \rightsquigarrow O(n)$, probability upscaled by $\frac{n \cdot (n-1)}{2} / [\frac{n}{2}]$



- > for all *n* super-droplets in a grid box of volume ΔV in timestep Δt
- \triangleright each representing ξ real particles (aerosol/cloud/drizzle/rain)

$$P_{ij} = max(\xi_i, \xi_j) \cdot \underbrace{\mathcal{E}(r_i, r_j) \cdot \pi(r_i + r_j)^2 \cdot |v_i - v_j|}_{\mathcal{E}(r_i, r_j)} \cdot \frac{\Delta t}{\Delta V} \cdot \frac{n \cdot (n-1)}{2} / \left[\frac{n}{2}\right]$$

coalescence kernel

where r = drop radii, $E(r_i, r_j) = collection efficiency, <math>v = drop$ velocities

- coalescence takes place once in a number of timesteps (def. by P_{ij}) all min (ξ_i, ξ_j) droplets coalesce \rightarrow there's always a "bin" of the right size to store the collided particl
- \blacktriangleright collisions triggered by comparing a uniform random number with P_{ij}
- ▶ extensive parameters summed (~→ conserved), intensive averaged
- ▶ [n/2] random non-overlapping (i,j) pairs examined only cost: $O(n^2) \rightsquigarrow O(n)$, probability upscaled by $\frac{n \cdot (n-1)}{2} / [\frac{n}{2}]$



- ▷ for all *n* super-droplets in a grid box of volume ΔV in timestep Δt
- \triangleright each representing ξ real particles (aerosol/cloud/drizzle/rain)
- ▶ the probability of coalescence of i-th and j-th super-droplets is:

$$\mathcal{P}_{ij} = max(\xi_i, \xi_j) \cdot \underbrace{\mathcal{E}(r_i, r_j) \cdot \pi(r_i + r_j)^2 \cdot |v_i - v_j|}_{\text{coalescence kernel}} \cdot \frac{\Delta t}{\Delta V}$$

where r - drop radii, $E(r_i, r_j) - \text{collection efficiency}$, v - drop velocities

- coalescence takes place once in a number of timesteps (def. by P_{ij}) all min (ξ_i, ξ_j) droplets coalesce \rightarrow there's always a "bin" of the right size to store the collided particle
- collisions triggered by comparing a uniform random number with P_{ij}
- \blacktriangleright extensive parameters summed (\rightsquigarrow conserved), intensive averaged
- ▶ [n/2] random non-overlapping (i,j) pairs examined only cost: $O(n^2) \rightsquigarrow O(n)$, probability upscaled by $\frac{n \cdot (n-1)}{2} / [\frac{n}{2}]$



- ▷ for all *n* super-droplets in a grid box of volume ΔV in timestep Δt
- \triangleright each representing ξ real particles (aerosol/cloud/drizzle/rain)
- ▶ the probability of coalescence of i-th and j-th super-droplets is:

$$P_{ij} = max(\xi_i, \xi_j) \cdot \underbrace{E(r_i, r_j) \cdot \pi(r_i + r_j)^2 \cdot |v_i - v_j|}_{\text{coalescence kernel}} \cdot \frac{\Delta t}{\Delta V} \quad \text{for all the second s$$

where r - drop radii, $E(r_i, r_i) - collection efficiency, <math>v - drop$ velocities

- \triangleright coalescence takes place once in a number of timesteps (def. by P_{ij})
- ► all min(ξ_i,ξ_j) droplets coalesce → there's always a "bin" of the right size to store the collided particles
- \blacktriangleright collisions triggered by comparing a uniform random number with P_{ij}
- ▶ extensive parameters summed (~→ conserved), intensive averaged
- ▶ [n/2] random non-overlapping (i,j) pairs examined only cost: $O(n^2) \rightsquigarrow O(n)$, probability upscaled by $\frac{n \cdot (n-1)}{2} / [\frac{n}{2}]$



- ▷ for all *n* super-droplets in a grid box of volume ΔV in timestep Δt
- \triangleright each representing ξ real particles (aerosol/cloud/drizzle/rain)
- ▶ the probability of coalescence of i-th and j-th super-droplets is:

$$P_{ij} = max(\xi_i, \xi_j) \cdot \underbrace{E(r_i, r_j) \cdot \pi(r_i + r_j)^2 \cdot |v_i - v_j|}_{\text{coalescence kernel}} \cdot \frac{\Delta t}{\Delta V}$$

where r - drop radii, $E(r_i, r_i) - collection efficiency, <math>v - drop$ velocities

- \triangleright coalescence takes place once in a number of timesteps (def. by P_{ij})
- ► all min(ξ_i,ξ_j) droplets coalesce → there's always a "bin" of the right size to store the collided particles
- \triangleright collisions triggered by comparing a uniform random number with P_{ij}
- ▶ extensive parameters summed (~→ conserved), intensive averaged
- ▶ [n/2] random non-overlapping (i,j) pairs examined only cost: $O(n^2) \rightsquigarrow O(n)$, probability upscaled by $\frac{n \cdot (n-1)}{2} / [\frac{n}{2}]$



- ▷ for all *n* super-droplets in a grid box of volume ΔV in timestep Δt
- \triangleright each representing ξ real particles (aerosol/cloud/drizzle/rain)
- ▶ the probability of coalescence of i-th and j-th super-droplets is:

$$P_{ij} = max(\xi_i, \xi_j) \cdot \underbrace{E(r_i, r_j) \cdot \pi(r_i + r_j)^2 \cdot |v_i - v_j|}_{\text{coalescence kernel}} \cdot \frac{\Delta t}{\Delta V}$$

where r - drop radii, $E(r_i, r_i) - collection efficiency, <math>v - drop$ velocities

- \triangleright coalescence takes place once in a number of timesteps (def. by P_{ij})
- ► all min (ξ_i, ξ_j) droplets coalesce \rightsquigarrow there's always a "bin" of the right size to store the collided particles
- \triangleright collisions triggered by comparing a uniform random number with P_{ij}
- ▶ extensive parameters summed (~→ conserved), intensive averaged
- ▶ [n/2] random non-overlapping (i,j) pairs examined only cost: $O(n^2) \rightsquigarrow O(n)$, probability upscaled by $\frac{n \cdot (n-1)}{2} / [\frac{n}{2}]$



- ▷ for all *n* super-droplets in a grid box of volume ΔV in timestep Δt
- \triangleright each representing ξ real particles (aerosol/cloud/drizzle/rain)
- ▶ the probability of coalescence of i-th and j-th super-droplets is:

$$P_{ij} = max(\xi_i, \xi_j) \cdot \underbrace{E(r_i, r_j) \cdot \pi(r_i + r_j)^2 \cdot |v_i - v_j|}_{\text{coalescence kernel}} \cdot \frac{\Delta t}{\Delta V} \cdot \frac{n \cdot (n-1)}{2} / \begin{bmatrix} n \\ 2 \end{bmatrix}$$

where r - drop radii, $E(r_i, r_i) - \text{collection efficiency}$, v - drop velocities

- \triangleright coalescence takes place once in a number of timesteps (def. by P_{ij})
- ► all min (ξ_i, ξ_j) droplets coalesce \rightsquigarrow there's always a "bin" of the right size to store the collided particles
- \triangleright collisions triggered by comparing a uniform random number with P_{ij}
- ▶ extensive parameters summed (~→ conserved), intensive averaged
- ▷ [n/2] random non-overlapping (i,j) pairs examined only cost: $O(n^2) \rightsquigarrow O(n)$, probability upscaled by $\frac{n \cdot (n-1)}{2} / [\frac{n}{2}]$





background: Figure 1. from Rauber et al. 2007 (MWR)



Simulation set-up[s]

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- ▶ domain size: 6.4 × 6.4 × 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- initial $u, v, q_t, \& \theta_l$ profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μ m in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\blacktriangleright~~64~\times~~64~\times~100$ ("coarse"): 8, 32, 128, 512
 - ▶ 128 × 128 × 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32

Simulation set-up[s]

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- ▶ domain size: 6.4 × 6.4 × 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- initial $u, v, q_t, \& \theta_l$ profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μ m in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\blacktriangleright~$ 64 $\times~$ 64 $\,\times$ 100 ("coarse"): 8, 32, 128, 512
 - ▶ 128 × 128 × 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32
- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- $\triangleright\,$ domain size: 6.4 \times 6.4 \times 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- initial u, v, q_t , & θ_l profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μ m in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\blacktriangleright~~64~\times~~64~\times~100$ ("coarse"): 8, 32, 128, 512
 - ▶ 128 × 128 × 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- $\triangleright\,$ domain size: 6.4 \times 6.4 \times 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- initial u, v, q_t , & θ_l profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μ m in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\blacktriangleright~$ 64 $\times~$ 64 $\,\times~$ 100 ("coarse"): 8, 32, 128, 512
 - ▶ 128 × 128 × 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- $\triangleright\,$ domain size: 6.4 \times 6.4 \times 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- initial u, v, q_t , & θ_l profiles & large-scale forcings based on observations
 - coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μ m in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\blacktriangleright~$ 64 $\times~$ 64 $\,\times$ 100 ("coarse"): 8, 32, 128, 512
 - ▶ 128 × 128 × 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- $\triangleright\,$ domain size: 6.4 \times 6.4 \times 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- ▷ initial u, v, q_t , & θ_l profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μ m in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\blacktriangleright~$ 64 $\times~$ 64 $\,\times~$ 100 ("coarse"): 8, 32, 128, 512
 - ▶ 128 × 128 × 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- $\triangleright\,$ domain size: 6.4 \times 6.4 \times 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- initial u, v, q_t , & θ_l profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- \triangleright initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μm in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\triangleright~~64~\times~~64~\times~100$ ("coarse"): 8, 32, 128, 512
 - ▶ 128 × 128 × 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- $\triangleright\,$ domain size: 6.4 \times 6.4 \times 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- ▷ initial u, v, q_t , & θ_l profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- \triangleright initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μm in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\sim~64~\times~64~\times$ 100 ("coarse"): 8, 32, 128, 512
 - \sim 128 \times 128 \times 200 ("middle"): 8, 32, 128
 - ≥ 256 × 256 × 400 ("high"): 8, 32

- LES solver: Nagoya Univ. CReSS (Tsuboki et al.) at the Earth Simulator 2
- duration: 24h (analyses over the last 4h)
- $\triangleright\,$ domain size: 6.4 \times 6.4 \times 4.0 km (quarter of the size from original set-up)
- boundary conditions:
 - lateral: periodic
 - top: sponge layer
 - bottom: surfaces fluxes parameterised, constant SST
- ▷ initial u, v, q_t , & θ_l profiles & large-scale forcings based on observations
- coalescence kernel: Hall 1980 (i.e. no effects of turbulence)
- \triangleright initial particle spectrum: bimodal lognormal at equilibrium with ambient humidity, sampled randomly between 10 nm and 5 μm in radius
- grid sizes and mean super-droplet densities per grid cell:
 - $\succ~64~\times~64~\times~100$ ("coarse"): 8, 32, 128, 512
 - \sim 128 \times 128 \times 200 ("middle"): 8, 32, 128
 - ▶ 256 × 256 × 400 ("high"): 8, 32

Particle-based LES vs. other LES (van Zanten et al. 2011)



less sensitive to super-droplet density than to grid resolution

Particle-based LES vs. other LES (Matheou et al. 2011) $\leftarrow \Delta x=25,50,100 \text{ m}$ $\Delta x=20,40,80 \text{ m}$



cloud cover, LWP, RWP last 4 hours

Matheou et al. 2011, MWR: Fig. 8



FIG. 8. Time evolution of cloud cover, LWP, vertically integrated resolved-scale TKE, and surface precipitation rate for precipitating runs at different resolutions.

Focus of the analysis: mimicking particle-counting probes

Fast-FSSP:

 measures light scattered by single cloud particles
sizes cloud droplets in the 2-50 µm diameter range



Figure 1. from Rauber et al. 2007 (MWR)

OAP-2DS:

- measures light shadowed by cloud/drizzle/rain drops

- sizes multiple particles at a time in the 5-3000 μm diameter range



Fast-FSSP / Meteo-France, Toulouse Brenguier et al. 1997, JAOT



OAP-2DS / SPEC Inc. Boulder CO Lawson et al. 2006, JAOT

Focus of the analysis: mimicking particle-counting probes





▲□▶ ▲□▶ ▲臣▶ ▲臣▶ 臣 めの

(*) Q (*

- > Fast-FSSP spectral range (1-24 μ m in radius)
- ▶ Fast-FSSP concentration threshold (20 cm⁻³)
- ▷ 5th-95th percentile, interquartile, 45th-55th percentile ranges vs. height

- caveats:
 - last 4h of the LES vs. flight-long statistics
 - ▶ grid cell vol. (~10⁵m³) vs. Fast-FSSP sample vol. (10⁻⁶m³ @10Hz)
 - "typical conditions" vs. different flights/days
 - LES sensitivity to grid resolution & super-droplet density



- Fast-FSSP spectral range (1-24 μ m in radius)
- Fast-FSSP concentration threshold (20 cm⁻³)
- ▷ 5th-95th percentile, interquartile, 45th-55th percentile ranges vs. height



- last 4h of the LES vs. flight-long statistics
- ▶ grid cell vol. (~10⁵m³) vs. Fast-FSSP sample vol. (10⁻⁶m³ @10Hz)
- "typical conditions" vs. different flights/days
- LES sensitivity to grid resolution & super-droplet density



- Fast-FSSP spectral range (1-24 μ m in radius)
- Fast-FSSP concentration threshold (20 cm⁻³)
- ▶ 5th-95th percentile, interquartile, 45th-55th percentile ranges vs. height



- last 4h of the LES vs. flight-long statistics
- ▶ grid cell vol. (~10⁵m³) vs. Fast-FSSP sample vol. (10⁻⁶m³ @10Hz)
- "typical conditions" vs. different flights/days
- LES sensitivity to grid resolution & super-droplet density



- Fast-FSSP spectral range (1-24 μ m in radius)
- Fast-FSSP concentration threshold (20 cm⁻³)
- > 5th-95th percentile, interquartile, 45th-55th percentile ranges vs. height



- last 4h of the LES vs. flight-long statistics
- $\,\triangleright\,$ grid cell vol. (${\sim}10^5 m^3)$ vs. Fast-FSSP sample vol. (10^{-6} m^3 @10Hz)
- "typical conditions" vs. different flights/days
- LES sensitivity to grid resolution & super-droplet density



- Fast-FSSP spectral range (1-24 μ m in radius)
- Fast-FSSP concentration threshold (20 cm⁻³)
- > 5th-95th percentile, interquartile, 45th-55th percentile ranges vs. height



- last 4h of the LES vs. flight-long statistics
- sprid cell vol. ($\sim 10^5 m^3$) vs. Fast-FSSP sample vol. ($10^{-6} m^3$ @10Hz)
- "typical conditions" vs. different flights/days
- LES sensitivity to grid resolution & super-droplet density



- Fast-FSSP spectral range (1-24 μ m in radius)
- Fast-FSSP concentration threshold (20 cm⁻³)
- > 5th-95th percentile, interquartile, 45th-55th percentile ranges vs. height



- last 4h of the LES vs. flight-long statistics
- sprid cell vol. ($\sim 10^5 m^3$) vs. Fast-FSSP sample vol. ($10^{-6} m^3$ @10Hz)
- "typical conditions" vs. different flights/days
- LES sensitivity to grid resolution & super-droplet density





- lowest quartile subsaturated
- maximum near cloud base (median profile) ~> CCN activation kinetics
- \triangleright condensational growth integrated implicitly $ightarrow \Delta t \sim$ 0.2 s
- values: lack of measurements to compare to?





- lowest quartile subsaturated
- ▶ maximum near cloud base (median profile) ~→ CCN activation kinetics
- \blacktriangleright condensational growth integrated implicitly $\rightsquigarrow \Delta t \sim$ 0.2 s
- values: lack of measurements to compare to?



- lowest quartile subsaturated
- ▶ maximum near cloud base (median profile) ~→ CCN activation kinetics
- \triangleright condensational growth integrated implicitly $\rightsquigarrow \Delta t \sim$ 0.2 s
- values: lack of measurements to compare to?



- lowest quartile subsaturated
- ▶ maximum near cloud base (median profile) ~→ CCN activation kinetics
- $\,\triangleright\,$ condensational growth integrated implicitly $\rightsquigarrow\,\Delta t\sim$ 0.2 s
- values: lack of measurements to compare to?



- values comparable with RICO data (measurements: day-to-day variability!)
- measurements: increase with height? (vigorous updraft \sim deeper & higher conc





- values comparable with RICO data (measurements: day-to-day variability!)
- roughly constant with height (precip sink in the upper part)

 \sim measurements: increase with height? (vigorous updraft \rightsquigarrow deeper & higher conc.)





- values comparable with RICO data (measurements: day-to-day variability!)
- roughly constant with height (precip sink in the upper part)
- \blacktriangleright measurements: increase with height? (vigorous updraft \rightsquigarrow deeper & higher conc.)





reasons for the reduced slope in the upper part of the cloud field:

- the Fast-FSSP 1–24 μm drop radius range
 - decreased efficiency, in terms of radius change, of condensational growth
- increased probability of drop collisions and coalescence





reasons for the reduced slope in the upper part of the cloud field:

- ▷ the Fast-FSSP 1–24 μ m drop radius range
- b decreased efficiency, in terms of radius change, of condensational growth

increased probability of drop collisions and coalescence





reasons for the reduced slope in the upper part of the cloud field:

- ▷ the Fast-FSSP 1–24 μ m drop radius range
- b decreased efficiency, in terms of radius change, of condensational growth
- increased probability of drop collisions and coalescence











LWC (g m⁻⁰)

Fig. 4. Scatterplot of $\langle k \rangle$ values as function of the LWC adiabatic fraction. For the LWC adiabatic fraction, the difference between the 80th and the 20th percentile of the frequency distribution is used

Super-Droplet LES vs. RICO Fast-FSSP measurements



> values larger than in adiabatic growth (~> mixing-induced broadening)

highest percentile profiles correspond to measurements (increase with height) drop breakup and influences of turbulence not represented in the model





- ▶ values larger than in adiabatic growth (~→ mixing-induced broadening)
- highest percentile profiles correspond to measurements (increase with height)
- drop breakup and influences of turbulence not represented in the mode





- ▶ values larger than in adiabatic growth (~→ mixing-induced broadening)
- highest percentile profiles correspond to measurements (increase with height)
- b drop breakup and influences of turbulence not represented in the model



Focus of the analysis: mimicking particle-counting probes


OAP-2DS-mimicking analysis vs. RICO OAP-2DS statistics Baker et al. 2009, JAMC

BAKER ET AL

MARCH 2009



FIG. 4. The mean of 237 rain PSDs is shown on top of density contours of the 237 individual rain PSDs observed at 600-ft (~183 m) altitude over the ocean on 19 Jan 2005. The contours show the number of PSDs passing through the region. Very few individual PSDs have any counts at all between 30 and 100 µm. These do not appear on the contour plot because zero values are not included on log-log plots. showing the conc μ m are e centration particles complete The meas than 100 through e is slow re tion and also prese the remo and splas

Acknow Bjorn Ste outstandi field pha: NSF Gra develope the Offic School C Aircraft tion for t RF17 (Jan. 19th 2005)

- 237 size distributions (line=mean)
- observed in rain shafts at 180 m (600 ft)
 cloud base at 0.5 km (1.6 kft)



OAP-2DS-mimicking analysis vs. RICO OAP-2DS statistics



OAP-2DS-mimicking analysis vs. RICO OAP-2DS statistics Baker et al. 2009, JAMC

MARCH 2009





Fig. 4. The mean of 237 rain PSDs is shown on top of density contours of the 237 individual rain PSDs observed at 600-ft (~183 m) altitude over the ocean on 19 Jan 2005. The contours show the number of PSDs passing through the region. Very few individual PSDs have any counts at all between 30 and 100 μ m. These do not appear on the contour plot because zero values are not included on log–log plots. showing 1 The conc μ m are e centratio particles complete The meas than 100 through e is slow re tion and also press the remc and splas

Acknoi Bjorn Ste outstandi field pha NSF Gra develope the Offic School C Aircraft tion for t

- Fair agreement for d>100 μ m (best for highest SD densities)
- no agreement for 10–20 µm where the OAP-2DS measured: "most likely deliquesced aerosols"
- no aerosol sources in the model (analysis: last 4h of 24h runs)
- no drop breakup in the model

Summary

- > salient features of the Super-Droplet μ -physics:
 - diffusive error-free computational schemes for both condensational and collisional growth
 - linear scaling of computational cost with the number of particles
 - persistence of arbitrary number of scalar quantities assigned to a super-droplet (e.g. chemical properties)
- (arguably) reasonable agreement with in-situ measurements
 set-up includes the key players in aerosol-cloud-precip interactions
- fewer parameterisation in comparison with bulk or bin models (e.g. Köhler curve and aerosol size spectrum instead of activation parameterisations or autoconversion thresholds)



- processed CCN formed by evaporation of
 - collisionally-grown drops
 - drops within which irreversible oxidation occurred
- CCN spectrum modification by wet deposition
- simulations using a 2D kinematic framework with
 Wojciech Grabowski & Zach Lebo @ NCAR and
 Anna Jaruga @ Univ. Warsaw (visiting NCAR in January)





- processed CCN formed by evaporation of
 - collisionally-grown drops
 - drops within which irreversible oxidation occurred
- CCN spectrum modification by wet deposition
- simulations using a 2D kinematic framework with
 Wojciech Grabowski & Zach Lebo @ NCAR and
 Anna Jaruga @ Univ. Warsaw (visiting NCAR in January)





- processed CCN formed by evaporation of
 - collisionally-grown drops
 - drops within which irreversible oxidation occurred
- CCN spectrum modification by wet deposition
- simulations using a 2D kinematic framework with
 Wojciech Grabowski & Zach Lebo @ NCAR and
 Anna Jaruga @ Univ. Warsaw (visiting NCAR in January)





- processed CCN formed by evaporation of
 - collisionally-grown drops
 - drops within which irreversible oxidation occurred
- CCN spectrum modification by wet deposition
- simulations using a 2D kinematic framework with
 Wojciech Grabowski & Zach Lebo @ NCAR and
 Anna Jaruga @ Univ. Warsaw (visiting NCAR in January)





- processed CCN formed by evaporation of
 - collisionally-grown drops
 - drops within which irreversible oxidation occurred
- CCN spectrum modification by wet deposition
- simulations using a 2D kinematic framework with
 Wojciech Grabowski & Zach Lebo @ NCAR and
 Anna Jaruga @ Univ. Warsaw (visiting NCAR in January)



Thanks for your attention!

Acknowledgements:

Hanna Pawłowska (University of Warsaw)

Kanya Kusano (JAMSTEC & Nagoya University)

Kozo Nakamura (JAMSTEC)

Computer time on the Earth Simulator 2 provided by JAMSTEC

Visit to NCAR funded by the Foundation for Polish Science



run label	grid	dx=dy	dz	time-steps [s]	SD density $[cm^{-3}]$
blk-coarse	$64 \times 64 \times 100$	100m	40m	1.00/0.100 n/a	n/a
sdm-coarse-8	$64 \times 64 \times 100$	100m	40m	1.00/0.100/0.25/1.0/1.0	2.0×10^{-11}
sdm-coarse-32	$64 \times 64 \times 100$	100m	40m	1.00/0.100/0.25/1.0/1.0	8.0×10^{-11}
sdm-coarse-128	$64 \times 64 \times 100$	100m	40m	1.00/0.100/0.25/1.0/1.0	3.2×10^{-10}
sdm-coarse-512	$64 \times 64 \times 100$	100m	40m	1.00/0.100/0.25/1.0/1.0	1.3×10^{-09}
sdm-middle-8	$128 \times 128 \times 200$	50m	20m	0.50/0.050/0.25/1.0/1.0	1.6×10^{-10}
sdm-middle-32	$128 \times 128 \times 200$	50m	20m	0.50/0.050/0.25/1.0/1.0	6.4×10^{-10}
sdm-middle-128	$128 \times 128 \times 200$	50m	20m	0.50/0.050/0.25/1.0/1.0	2.6×10^{-09}
sdm-high-8	$256 \times 256 \times 400$	25m	10m	0.25/0.025/0.25/1.0/0.5	1.3×10^{-09}
sdm-high-32	$256{\times}256{\times}400$	25m	10m	0.20/0.020/0.20/1.0/0.2	5.1×10^{-09}





UNI PAROT

◆ロ▶ ◆昼▶ ◆臣▶ ◆臣▶ ─ 臣 ─ のへの



UNI Red of TRA

- □ ▶ ▲ 圖 ▶ ▲ 圖 ▶ ▲ 圖 ▶ ▲ 圖 ● の Q @







sdm-coarse-128

1.6

1.4

height [m]

height [m]

. .