

On the Role of Wind Shear and Cloud Droplet Sedimentation on Entrainment in Stratocumulus

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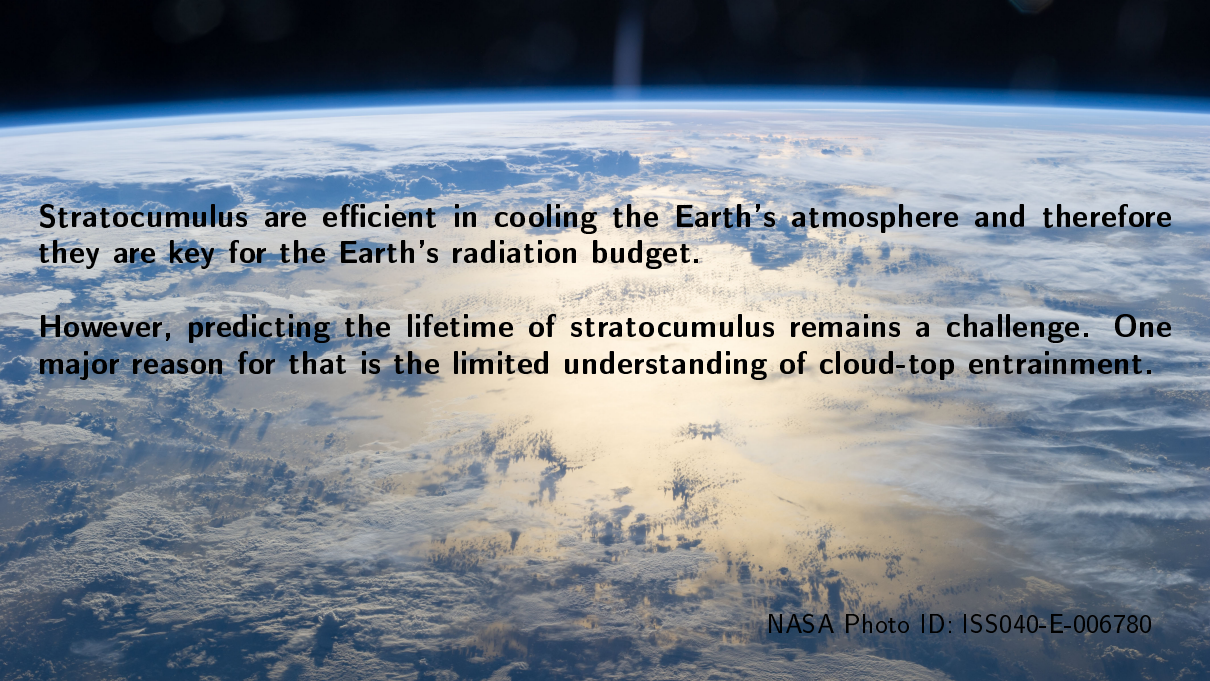
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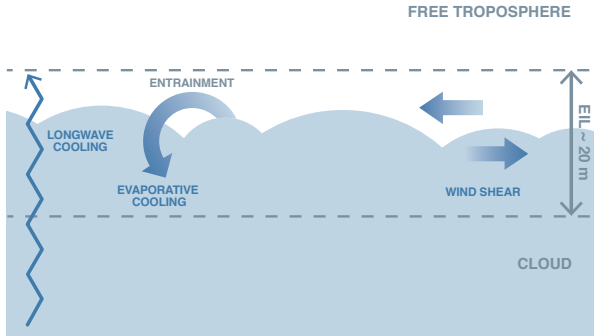


Stratocumulus are efficient in cooling the Earth's atmosphere and therefore they are key for the Earth's radiation budget.

However, predicting the lifetime of stratocumulus remains a challenge. One major reason for that is the limited understanding of cloud-top entrainment.

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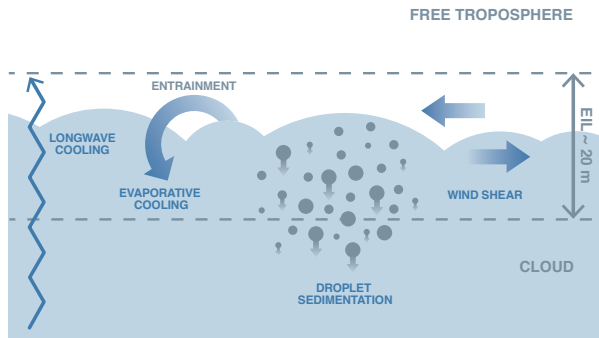
Quantifying wind-shear effects remains a challenge



The EIL is a transition layer between the cloud and the free troposphere.

- Wind shear can substantially enhance entrainment and thicken the entrainment interfacial layer (EIL).
- At which minimal shear strength does shear start to enhance entrainment?
- The magnitude of shear enhancement remains highly uncertain.

Quantifying droplet-sedimentation effects remains a challenge

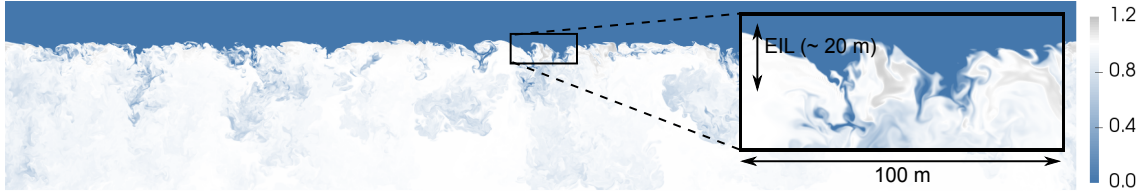


The EIL is a transition layer between the cloud and the free troposphere.

- Droplet sedimentation can substantially weaken entrainment.
- The magnitude of sedimentation weakening remains highly uncertain (entrainment weakens by 5 – 40% *).
- To what extent can sedimentation and shear effects compensate each other?
- How do sedimentation and shear effects compensate each other?

Direct numerical simulations resolve mixing processes in the EIL

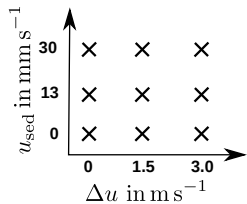
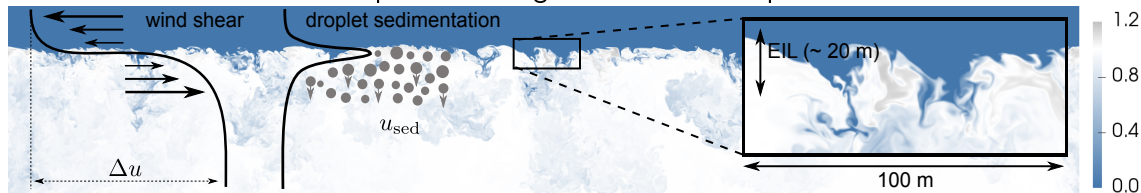
Simulation snapshot showing the normalized liquid water field:



- Direct numerical simulations of a nocturnal stratocumulus cloud-top are performed.
- Neglecting surface fluxes, drizzle, and solar heating allows us to reach submeter-scale resolution, i.e. $\Delta x = \Delta y = \Delta z \simeq 20$ cm.
- Match all atmospheric parameters of subtropical clouds (RF01 DYCOMS-II), except the Reynolds number. However, a certain degree of Reynolds number similarity is observed.

Systematic study of wind-shear and droplet-sedimentation effects

Simulation snapshot showing the normalized liquid water field:



- The cloud-top velocity jump Δu is varied.
- The bulk sedimentation velocity u_{sed} is varied.
- $u_{sed} = u_{sed}(d, \sigma_{gc})$ is a function of the mean droplet diameter d and of the geometric standard deviation σ_{gc} of the log-normal droplet size distribution *.

Research questions – Outline

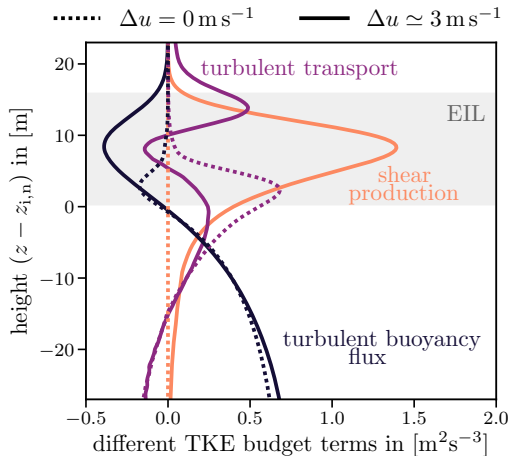
In general:

Direct numerical simulations are employed to better understand how wind shear and droplet sedimentation alter cloud-top entrainment.

In particular:

- (1) **At which minimal shear strength does shear start to enhance entrainment?**
- (2) To what extent can sedimentation and shear effects compensate each other?
- (3) How do sedimentation and shear compensate each other?

Two competing processes determine cloud-top entrainment

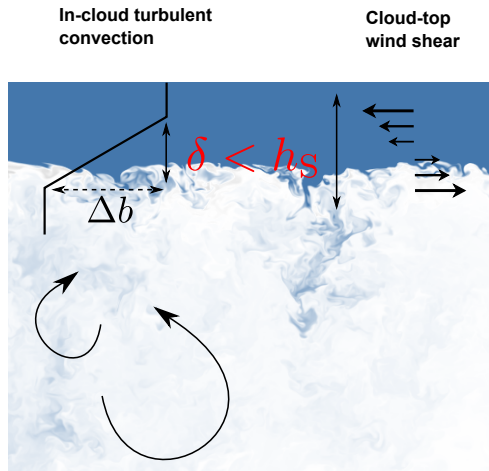


The budget of turbulent kinetic energy (TKE) in a quasi-steady state:

$$0 \simeq -\partial_z T + P + B - \epsilon.$$

- $\Delta u = 0 \text{ m s}^{-1}$: the **turbulent transport term** $-\partial_z T$ dominates.
- $\Delta u \simeq 3 \text{ m s}^{-1}$: the **shear production term** P dominates.

Two competing processes determine cloud-top entrainment



Δb is the cloud-top buoyancy jump

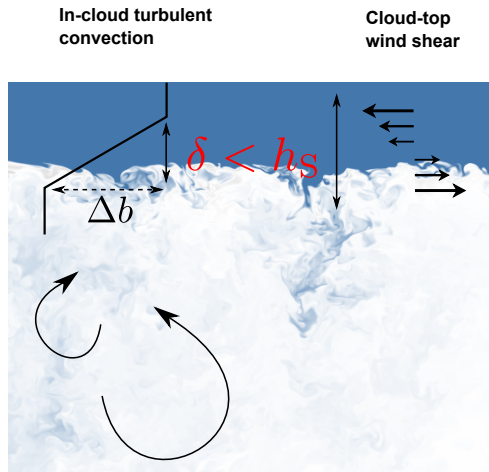
1. Penetrations of in-cloud turbulent convection into the stably stratified EIL are characterized by the penetration depth δ .
2. Shear driven turbulence is characterized by the shear layer thickness $h_S = (\Delta u)^2 / (3\Delta b)$.

Convection dominates for: $\delta \gg h_S$

Shear dominates for: $\delta \ll h_S$

This suggests to define $h_S = \delta_{\text{crit}}$ as a critical value.

Shear enhances cloud-top entrainment only for $\Delta u > (\Delta u)_{\text{crit}}$



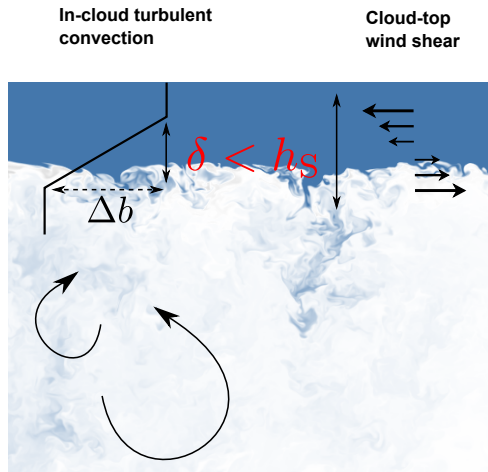
Δb is the cloud-top buoyancy jump

But how to estimate δ ? Balance of potential and kinetic energy:

$$\begin{aligned} E_{\text{pot}} &= E_{\text{kin}} \\ \delta \frac{\delta \Delta b}{h_s} &= \alpha_1 w_*^2 + \alpha_2 \left(\delta \frac{\Delta u}{h_s} \right)^2 \\ \Rightarrow \delta &= \sqrt{\frac{\alpha_1}{3(2 - 3\alpha_2)}} \frac{\Delta u w_*}{\Delta b} \\ \delta &\simeq 1.4 \frac{\Delta u w_*}{\Delta b}, \end{aligned}$$

where the *convective velocity scale* w_* characterizes the strength of in-cloud turbulence and $h_s = (\Delta u)^2 / (3\Delta b)$.

Shear enhances cloud-top entrainment only for $\Delta u > (\Delta u)_{\text{crit}}$



Δb is the cloud-top buoyancy jump

$$\delta \simeq 1.4(\Delta u w_*)/\Delta b \quad \text{and} \quad h_S = (\Delta u)^2/3\Delta b$$

Substituting these expressions in the threshold condition $h_S = \delta_{\text{crit}}$ yields

$$(\Delta u)_{\text{crit}} \simeq 4w_*,$$

which implies for $w_* \simeq 0.18 - 0.92 \text{ m s}^{-1}$ *

$$(\Delta u)_{\text{crit}} \simeq 1 - 4 \text{ m s}^{-1}.$$

Can wind shear weaken in-cloud turbulence w_* ?

Definition of $(\Delta u)_{\text{crit}} \simeq 4w_*$ suggests that w_* is independent of Δu .

However, previous studies* indicate that wind shear can weaken in-cloud turbulence w_* .

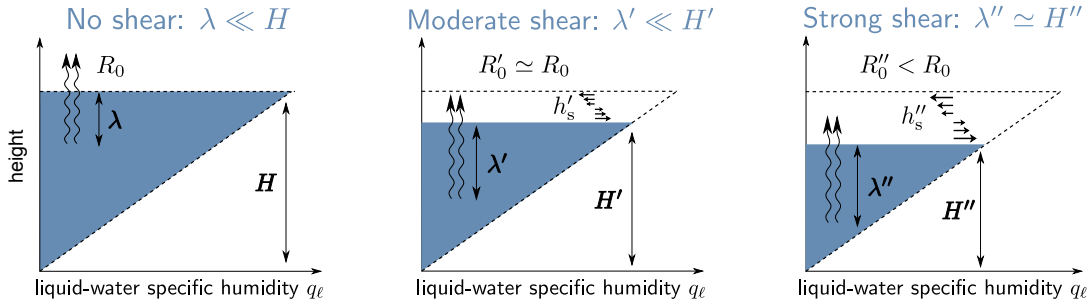
Basic idea: Shear enhanced evaporation reduces the liquid-water specific humidity q_ℓ , which reduces the net radiative cooling R_0 and weakens in-cloud turbulence w_* .

Shear enhanced evaporation does not necessarily weaken in-cloud turbulence.

Only a shear with $\Delta u > (\Delta u)_{\text{dep}}$ weakens in-cloud turbulence

Redefined idea:

R_0 net radiative cooling, λ extinction length, H cloud depth. Moreover $\lambda \sim q_{\ell, \text{max}}^{-1} d_0$

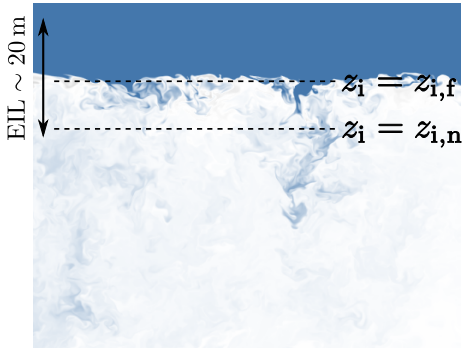


Formalizing this line of argumentation yields a depletion velocity jump of $(\Delta u)_{\text{dep}}(H) \simeq 4 - 10 \text{ m s}^{-1}$.

Research questions – Outline

- (1) At which minimal shear strength does shear start to enhance entrainment?
 - Only a cloud-top wind shear with $\Delta u > (\Delta u)_{\text{crit}} \simeq 1 - 4 \text{ m s}^{-1}$ enhances entrainment.
 - Only a wind shear with $\Delta u > (\Delta u)_{\text{dep}} \simeq 4 - 10 \text{ m s}^{-1}$ weakens in-cloud turbulence.
- (2) **To what extent can sedimentation and shear effects compensate each other?**
- (3) How do sedimentation and shear compensate each other?

Definition of the entrainment velocity w_e



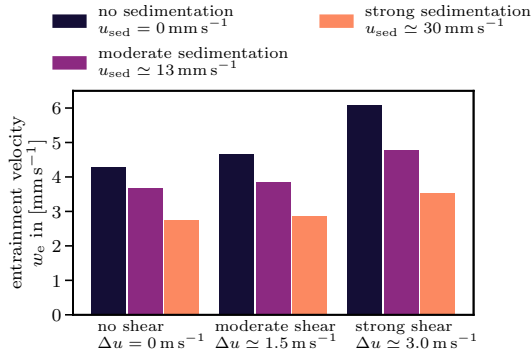
The entrainment velocity

$$w_e = \frac{dz_i}{dt}$$

quantifies the rate of mixing between cloudy and free-tropospheric air.

- Different definitions of the reference height z_i are used.

Sedimentation and shear effects can compensate each other



- Droplet sedimentation weakens entrainment by up to 40%. (LES studies typically report 5 – 25% *.)
- A strong shear exceeding $(\Delta u)_{\text{crit}} \simeq 2.5 \text{ m s}^{-1}$ enhances entrainment by up to 40%.

Entrainment can be equally sensitive towards changes in wind shear and towards changes in the droplet size distribution.

Entrainment can be equally sensitive towards changes in wind-shear and in the droplet size distribution

Implications:

- Changes in the droplet size distribution can substantially affect cloud lifetimes not only because of its effect on rain formation, but also because of its effect on cloud-top entrainment.
- A better characterization of the droplet size distribution is needed to accurately represent mixing effects on cloud lifetimes.

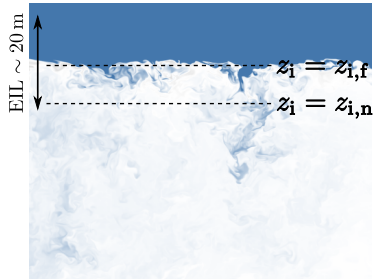
Research Questions – Summary

- (1) At which minimal shear strength does shear start to enhance entrainment?
 - Only a cloud-top wind shear with $\Delta u > (\Delta u)_{\text{crit}} \simeq 1 - 4 \text{ m s}^{-1}$ enhances entrainment.
 - Only a wind shear with $\Delta u > (\Delta u)_{\text{dep}} \simeq 4 - 10 \text{ m s}^{-1}$ weakens in-cloud turbulence.
- (2) To what extent can sedimentation and shear effects compensate each other?
 - Sedimentation weakening can cancel shear enhancement, indicating that entrainment can be equally sensitive to changes in shear and to changes in the droplet size distribution.
- (3) **How do sedimentation and shear compensate each other?**

The entrainment rate equation

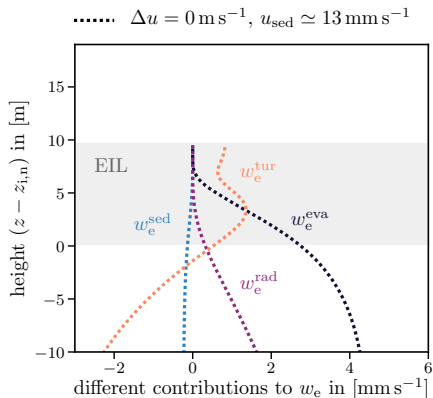
The entrainment velocity $w_e = dz_i/dt$ can be analytically decomposed into six contributions:

$$w_e = w_e^{\text{tur}} + w_e^{\text{eva}} + w_e^{\text{sed}} + w_e^{\text{rad}} + w_e^{\text{mol}} + w_e^{\text{def}}.$$



- The turbulent buoyancy flux contribution
 $w_e^{\text{tur}} \sim -\langle w'b' \rangle_{z_i}.$
- The evaporative cooling contribution
 $w_e^{\text{eva}} \sim (E_0 - \langle E \rangle_{z_i}).$
- The sedimentation buoyancy flux contribution
 $w_e^{\text{sed}} \sim -\langle \mathbf{j}_\mu g \cdot \mathbf{k} \rangle_{z_i}.$
- The radiative cooling contribution
 $w_e^{\text{rad}} \sim \beta(R_0 - \langle R \rangle_{z_i}).$

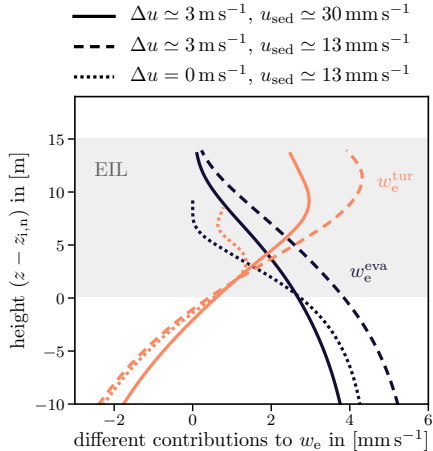
The different contributions to w_e vary strongly with height



$$w_e = w_e^{\text{tur}} + w_e^{\text{sed}} + w_e^{\text{eva}} + w_e^{\text{rad}} + w_e^{\text{mol}} + w_e^{\text{def}}$$

- Strong dependence on the reference height z_i .
- Contributions of w_e^{rad} and w_e^{sed} are small.
- However, total radiative cooling R_0 remains comparable to total evaporative cooling E_0 .

Sedimentation and shear compensate each other due to their opposing effects on w_e^{tur} and w_e^{eva}

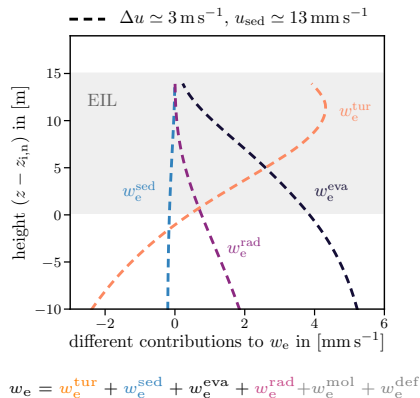


$$w_e = w_e^{\text{tur}} + w_e^{\text{sed}} + w_e^{\text{eva}} + w_e^{\text{rad}} + w_e^{\text{mol}} + w_e^{\text{def}}$$

- Shear amplifies w_e^{tur} & Shear enhanced entrainment amplifies w_e^{eva} .
- Sedimentation induced thickening of the EIL weakens w_e^{tur} & Sedimentation removes liquid water from the EIL, which weakens w_e^{eva} .

The way sedimentation and shear compensate each other depends strongly on height.

Three implications for entrainment velocity parametrizations



Mixed-layer models need accurate parameterizations of the entrainment velocity.

Implications:

1. Entrainment velocity parametrizations should pay equal attention to shear and sedimentation effects.
2. Separate contributions to w_e should be estimated at the same reference height z_i , even though different definitions of z_i only differ by a few meters.
3. Parameterizing w_e^{eva} and w_e^{tur} has priority (compared to w_e^{rad} and w_e^{sed}).

Research Questions – Summary

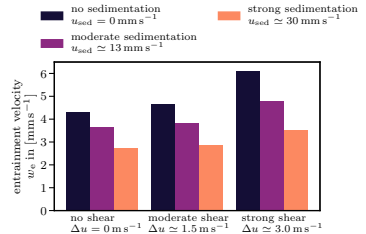
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- (2) To what extent can sedimentation and shear effects compensate each other?
 - Sedimentation weakening can cancel shear enhancement, indicating that entrainment can be equally sensitive to changes in shear and to changes in the droplet size distribution.
- (3) How do sedimentation and shear compensate each other?
 - Shear and sedimentation effects on w_e compensate each other due to their opposing effects on w_e^{tur} and w_e^{eva} . Changes in w_e^{sed} and w_e^{rad} are less important.
 - Different contributions to w_e depend strongly on the choice of the reference height z_i .

Take-home messages






Understanding and quantifying wind-shear and droplet-sedimentation effects on cloud-top entrainment is important but remains a challenge.

Conclusions:

1. Only a strong wind shear with $\Delta u > (\Delta u)_{\text{crit}} \simeq 4w_*$ enhances entrainment.
2. Entrainment reduction by droplet sedimentation can completely compensate entrainment enhancement by wind shear.
3. Shear and sedimentation effects on w_e compensate each other due to their opposing effects on w_e^{tur} and w_e^{eva} .
Even small variations of the reference height z_i matter.



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